



B.K. BIRLA CENTRE FOR EDUCATION

SARALA BIRLA GROUP OF SCHOOLS
A CBSE DAY-CUM-BOYS' RESIDENTIAL SCHOOL



POST MID TERM EXAMINATION 2025-26

APPLIED MATHEMATICS

MARKING KEY

Class: XI B

Date: 10/12/25

Admission no:

Time: 1hr

Max Marks: 25

Roll no:

General Instructions:

Question 1 to 5 carries ONE mark each. Questions 6 to 9 carries TWO marks each.
Questions 10 to 13 carries THREE marks each.

- $\lim_{x \rightarrow 2} \frac{\log(x-1)}{x-2}$ is equal to
a) 0 b) -1 c) 1/2 d) 1
- If $f(x) = \begin{cases} \frac{\sqrt{4+x}-2}{x} & x \neq 0 \\ k & x = 0 \end{cases}$ is continuous at $x = 0$, then the value of k is:
a) 1 b) 4 c) 1/4 d) 0
- If $y = \sqrt{x} + \frac{1}{\sqrt{x}}$, then dy/dx at $x=1$ is :
a) 1 b) 1/2 c) $1/\sqrt{2}$ d) 0
- The measure of central tendency of a statistical data which takes into account all the data is:
a) **Mean** b) Median c) Mode d) Range
- If $f(x) = \frac{(3x+1)(2\sqrt{x}-1)}{\sqrt{x}}$
a) **5** b) -5 c) 6 d) 11/2

- Find the derivative of the following function: $(ax+b)^2$

Sol: $\frac{dy}{dx} = 2(ax+b) \cdot a = 2a(ax+b)$.

- Differentiate the following function wrt $x: \sqrt{2x-3}$, $x > \frac{3}{2}$.

Sol: $\frac{dy}{dx} = \frac{1}{2\sqrt{2x-3}} \cdot 2 = \frac{1}{\sqrt{2x-3}}$

- The marks of 9 students in a test were 13, 17, 20, 5, 3, 3, 18, 15 and 20. Find the three quartile.

Sol: 3, 3, 5, 13, 15, 17, 18, 20, 20

$$Q1 = \frac{2nd \text{ observation} + 3rd \text{ observation}}{2} = \frac{8}{2} = 4$$

$$Q2 = 5^{th} \text{ observation} = 15$$

$$Q3 = \frac{7th \text{ observation} + 8th \text{ observation}}{2} = \frac{38}{2} = 19$$

- Find the mean and variance of first 10 multiples of 3.

Sol: 10 multiples of 3 : 3, 6, 9, 12, 15, 18, 21, 24, 27, 30

$n=10$,

Mean = $165/10 = 16.5$

Variance = $3456/10 - (16.5)^2 = 345.6 - 272.25 = 74.25$

10. Find the following limit: $\lim_{x \rightarrow 0} \frac{\sqrt{1+3x} - \sqrt{1-3x}}{x}$.

Sol; using rationalisation; $\lim_{x \rightarrow 0} \frac{(1+3x) - (1-3x)}{x\sqrt{1+3x} - \sqrt{1-3x}} = \lim_{x \rightarrow 0} \frac{6x}{x\sqrt{1+3x} - \sqrt{1-3x}} = \lim_{x \rightarrow 0} \frac{6}{\sqrt{1+3x} - \sqrt{1-3x}} = \frac{6}{2} = 3$

11. If $y = \sqrt{\log x + \sqrt{\log x + \sqrt{\log x + \cdots \infty}}}$, Prove that $x(2y-1) \frac{dy}{dx} = 1$.

Sol: $y = \sqrt{\log x + y}$

$y^2 = \log x + y$ diff. wrt x , we have $x(2y-1) \frac{dy}{dx} = 1$

12. Find the mean deviation about the mean of the following data:

Height in cm	95-105	105-115	115-125	125-135	135-145	145-155
No. of boys	9	13	26	30	12	10

Sol: Assumed mean (a) = 120, class size = 10, construction of proper table.

Mean = $120 + 5.3 = 125.3$

Mean deviation about mean = $1128.8/100 = 11.288 = 11.29$ (aprox)

13. Calculate the mean, variance and standard deviation of the following data:

Classes	30-40	40-50	50-60	60-70	70-80	80-90	90-100
Frequency	3	7	12	15	8	3	2

Sol: Assumed mean (A) = 65, construction of table;

Mean = $65 - 3 = 62$

Variance = $10500/50 - (-150/50)^2 = 210 - 9 = 201$.

Standard deviation = $\sqrt{201} = 14.18$ (aprox)

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